



# Bacteriophage self-counting in the presence of viral replication

Tianyou Yao<sup>a,b,c,d,1</sup> , Seth Coleman<sup>e,f,g,1</sup>, Thu Vu Phuc Nguyen<sup>a,b,c,d</sup> , Ido Golding<sup>a,b,c,d,e,2</sup> , and Oleg A. Igoshin<sup>e,g,2</sup>

<sup>a</sup>Verna and Marrs McLean Department of Biochemistry and Molecular Biology, Baylor College of Medicine, Houston, TX 77030; <sup>b</sup>Department of Physics, University of Illinois at Urbana–Champaign, Urbana, IL 61801; <sup>c</sup>Department of Microbiology, University of Illinois at Urbana–Champaign, Urbana, IL 61801; <sup>d</sup>Center for the Physics of Living Cells, University of Illinois at Urbana–Champaign, Urbana, IL 61801; <sup>e</sup>Center for Theoretical Biological Physics, Rice University, Houston, TX 77030; <sup>f</sup>Applied Physics Graduate Program, Rice University, Houston, TX 77005; and <sup>g</sup>Department of Bioengineering, Rice University, Houston, TX 77030

Edited by Terence Hwa, Department of Physics, University of California San Diego, La Jolla, CA; received March 2, 2021; approved November 4, 2021

**When host cells are in low abundance, temperate bacteriophages opt for dormant (lysogenic) infection. Phage lambda implements this strategy by increasing the frequency of lysogeny at higher multiplicity of infection (MOI). However, it remains unclear how the phage reliably counts infecting viral genomes even as their intracellular number increases because of replication. By combining theoretical modeling with single-cell measurements of viral copy number and gene expression, we find that instead of hindering lambda's decision, replication facilitates it. In a nonreplicating mutant, viral gene expression simply scales with MOI rather than diverging into lytic (virulent) and lysogenic trajectories. A similar pattern is followed during early infection by wild-type phage. However, later in the infection, the modulation of viral replication by the decision genes amplifies the initially modest gene expression differences into divergent trajectories. Replication thus ensures the optimal decision—lysis upon single-phage infection and lysogeny at higher MOI.**

bacteriophage | mathematical modeling | *E. coli* | cell-fate decision | single cell

Following genome entry into the host cell, temperate bacteriophages must choose between two developmental pathways (1). In the default lytic pathway, rapid viral replication typically culminates in the death of the host cell (lysis) and release of viral progeny. By contrast, in the lysogenic pathway, phages suppress their virulent functions and enter a dormant prophage state (1). To decide on the infected cell's fate, temperate phages assess the environmental abundance of potential hosts (1, 2). If susceptible host cells are scarce, then producing hundreds of new phages via the lytic pathway would be futile, and, instead, lysogeny should be chosen. To evaluate the relative abundance of viruses and cells, phages use diverse methods. Some achieve this by measuring the number of simultaneously coinfecting phages (multiplicity of infection, MOI) and increasing the frequency of lysogeny at higher MOI (3, 4). Other bacteriophages harness cell–cell communication to assess the frequency of virus–host encounters in their vicinity (5, 6). Notwithstanding the mechanism by which the measurement is performed, a regulatory circuit encoded by the virus must interpret a biological signal reflecting the relative abundance of viruses and host cells and use it to bias a decision between the two possible outcomes of infection.

Phage lambda, a temperate bacteriophage that infects *Escherichia coli*, has long served as the paradigm for viral self-counting (7–10). Direct measurements both in bulk (10, 11) and in single cells (12) demonstrated that a higher number of coinfecting phages increases the probability of lysogeny. Decades of experimental interrogation have resulted in a comprehensive genetic understanding of the virus and the identification of key players involved in the lambda postinfection decision (13–15). However, despite this detailed molecular knowledge of the underlying circuitry, our system-level understanding of how MOI drives the infection outcome is far from complete (12, 16, 17). In contrast to the two-gene “switch” governing lysogenic maintenance (18),

the network driving the lysis/lysogeny decision comprises multiple genes, regulating each other through diverse molecular interactions (13). The common theoretical view of the decision is that this genetic network is biased by MOI toward either of two attractors, one corresponding to lytic onset, another to lysogeny (7, 9, 16, 17, 19–22). However, the way this takes place varies between models. Further challenging our ability to decipher the circuit's function is the fact that, while the eventual gene expression patterns in lysis and lysogeny clearly differ, the initial gene expression cascade following infection appears indistinguishable for both pathways (23).

Complicating phages' task of measuring MOI—and our attempts to decipher how they do it—is the fact that the viral copy number is rapidly increasing inside the infected cell (Fig. 1). Phage replication begins within minutes of genome entry (22) and coincides with the expression of early genes in the decision circuit (23) (Fig. 2). In other words, the initial MOI, which the viral circuitry presumably attempts to measure (24, 25), is soon obfuscated by the presence of additional phage genomes in the cell. Elucidating how lambda succeeds in distinguishing the initial genome number from the instantaneous number present in the cell has remained a challenge partly because of experimental limitations. Within a population, single-cell MOI is broadly distributed (10, 12) (*SI Appendix, Fig. S1*), necessitating measurements at the level of the individually infected cell. However, simultaneous measurement of the viral copy number and the expression of

## Significance

**Viral dormancy, in which the infected cell is not killed but rather becomes the long-term residence of the parasite, is a hallmark of viruses across kingdoms from bacteriophages to HIV. When and how viruses decide to opt for this lifestyle remains mysterious. Phage lambda, which serves as a paradigm for viral dormancy, is reported to count the number of coinfecting viruses and then uses this value to assess the abundance of potential hosts and decide whether to become dormant. Here, we use a single-cell measurement of viruses and messenger RNA together with mathematical modeling to illuminate how lambda performs this task.**

Author contributions: T.Y., S.C., T.V.P.N., I.G., and O.A.I. designed research; T.Y., S.C., and T.V.P.N. performed research; T.Y., S.C., and T.V.P.N. contributed new reagents/analytic tools; T.Y., S.C., T.V.P.N., I.G., and O.A.I. analyzed data; and T.Y., S.C., T.V.P.N., I.G., and O.A.I. wrote the paper.

The authors declare no competing interest.

This article is a PNAS Direct Submission.

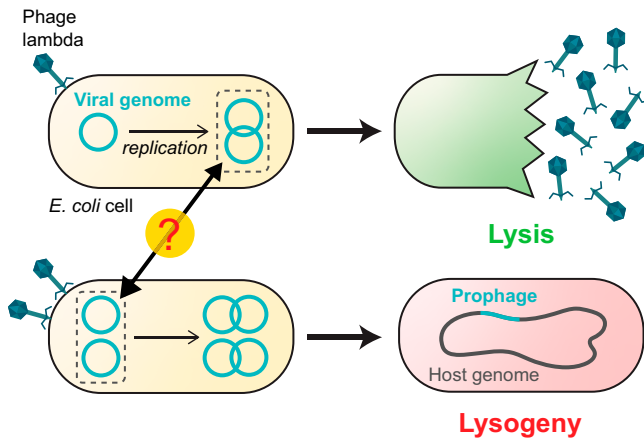
Published under the [PNAS license](#).

<sup>1</sup>T.Y. and S.C. contributed equally to this work.

<sup>2</sup>To whom correspondence may be addressed. Email: igolding@illinois.edu or igoshin@rice.edu.

This article contains supporting information online at <http://www.pnas.org/lookup/suppl/doi:10.1073/pnas.2104163118/-DCSupplemental>.

Published December 16, 2021.



**Fig. 1.** The lambda decision circuit measures the MOI even as the viral copy number is changing. A higher MOI increases the propensity to lysogenize. Here, infection by a single lambda phage (*Top*) results in lysis, whereas coinfection by two phages (*Bottom*) leads to lysogeny. In choosing cell fate, the infecting phage must respond to the initial number of viral genomes in the cell but ignore the subsequent increase in number because of viral replication.

phage genes has previously not been possible at single-cell resolution.

Here, we combine single-molecule detection of messenger RNA (mRNA) and phage genomes during infection with mathematical modeling of network dynamics to identify how lambda measures the number of coinfecting phages. To circumvent the complication of a time-varying genome number, we first examined infection by a replication-deficient lambda strain. At various times after infection, we measured, in individual cells, the viral copy number (which, in this case, equals the MOI) and mRNA levels of key lambda genes—*cI*, *cro*, and *cII*. To our surprise, we found no divergence of the mRNA trajectories between low and high MOI, indicative of a transition between the lytic and lysogenic attractors. Instead, gene expression simply scaled with viral dosage. This led us to hypothesize that viral replication is required for obtaining an MOI-dependent lysis/lysogeny decision. To test this hypothesis, we constructed a data-calibrated model for the decision network that included the coupling of phage replication to gene expression. Our model revealed that, indeed, viral replication is inextricably coupled to the lysogeny decision. Early in infection, during a time window set by the dynamics of CII, a short-lived activator, expression of the lysogenic repressor CI scales with MOI, similarly to what we observed in the absence of replication. However, subsequent replication—and its modulation by the decision genes—drive a sharp divergence of cell fates as a function of MOI. Specifically, the initial accumulation of CI at MOI > 1 leads to repression of both *cro* expression and viral replication, enabling the lysogenic choice. In contrast, at MOI = 1, accumulated CI is insufficient to repress *cro* expression and replication. Consequently, Cro production from a rapidly increasing number of *cro* gene copies activates the lytic pathway. We thus find that, rather than hindering lambda's decision by obscuring the initial MOI, viral replication ensures the appropriate choice of lysis upon infection by a single phage and lysogeny upon coinfection.

## Results

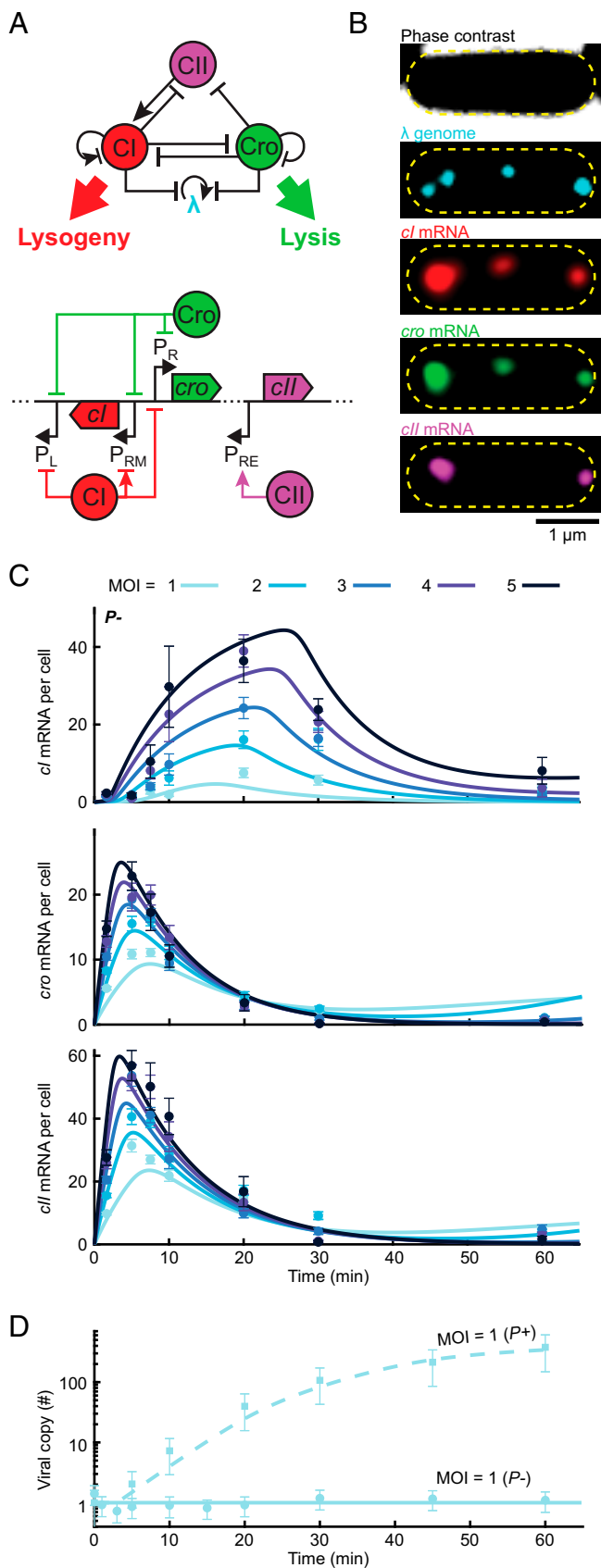
**In the Absence of Viral Replication, Gene Expression Does Not Diverge into Lytic and Lysogenic Trajectories.** To characterize the behavior of the lambda decision circuit, we sought to measure

gene expression kinetics during infection across a range of single-cell MOI values. To decouple the gene-regulatory aspects from the effects of time-varying dosage, we first followed the approach of Kourilsky (10) and Arkin et al. (7) and examined infection by a replication-deficient mutant (*Pam80*, henceforth denoted *P-*) (10). We focused on the expression of three lambda genes at the heart of the decision circuit—*cI*, *cro*, and *cII* (9, 19, 22) (Fig. 2A). Cro, transcribed from  $P_R$ , is a repressor that inhibits transcription of multiple lambda genes (including itself) from the two early promoters  $P_R$  and  $P_L$  (14). Cro is required for successful lysis to prevent the accumulation of CI and the overproduction of lambda proteins deleterious to later development (14). Transcription of *cro* can also be used as a proxy for the presence of Q, a critical lytic gene produced from the same polycistronic transcript (23). CI too inhibits transcription from  $P_R$  and  $P_L$  in addition to regulating its own expression from  $P_{RM}$  and is required for establishing and maintaining lysogeny (23). CII is a short-lived protein that activates early transcription of *cI* from  $P_{RE}$ , a critical event for the establishment of lysogeny (14). Both CI and Cro also suppress viral replication by inhibiting expression of the lambda replication proteins O and P (23) and by repressing transcription from  $P_R$ , required for early replication (13).

To measure the MOI dependence of expression dynamics in this three-gene subnetwork, we combined single-molecule quantification of mRNA and phage genomes in individual cells (26) (Fig. 2B). Following infection by a replication-deficient phage (*cl857 Pam80 P1parS*; refer to *SI Appendix, Experimental Methods and Tables S1–S6* for strain construction and experimental protocols), samples were taken at different time points and chemically fixed. The lambda genomes present in each cell were detected and counted using the ParB-*parS* system (27, 28) (*SI Appendix, Experimental Methods and Fig. S2*). In the same cells, mRNA copy numbers for *cI*, *cro*, and *cII* were measured using single-molecule fluorescence in situ hybridization (26, 29). The cells were then grouped based on the measured single-cell MOI, and the averaged mRNA level for each gene, time, and MOI was calculated (Fig. 2C).

All three genes exhibited a transient pulse of expression, with mRNA numbers first rising and then decaying (Fig. 2C). The main difference between genes was in the timing of the expression peak, with *cro* and *cII* reaching their highest level ~10 min after the entry of viral genomes and *cI* peaking later at about ~20 min. Biological replicates yielded consistent results (*SI Appendix, Fig. S3*). The observed dynamics were consistent with our current understanding of the gene expression cascade following infection (Fig. 2A): upon viral entry, *cro* and *cII* are transcribed from  $P_R$  (*SI Appendix, Figs. S4 and S5*), and this promoter is later repressed by Cro (23). *cI* transcription requires activation of the  $P_{RE}$  promoter and is hence delayed until enough CII protein, driving this activation, has accumulated (23).

Multiple theoretical models previously developed for the lysis/lysogeny decision have predicted distinct gene expression trajectories at low and high MOI, whereby in the former case, the lytic proteins accumulate while lysogenic ones remain low, and in the latter case, the reverse takes place (9, 16, 19–21). In light of this prevailing picture, we were surprised to observe no clear divergence of mRNA trajectories between low and high MOI, reflecting a transition from lysis to lysogeny. Instead, we found that for each of the genes, a simple scaling by a factor  $MOI^\epsilon$  [suggested previously by Joh and Weitz (16)], with  $\epsilon \approx 1$  for *cI* and  $\epsilon \approx 0.5$  for *cro* and *cII*, yielded a near collapse of the different MOI-gated trajectories to a single curve (*SI Appendix, Fig. S6*). Thus, gene expression kinetics following *P-* infection did not reveal a clear signature of a transition from lysis to lysogeny as MOI increases.



**Fig. 2.** A simplified model of the decision network captures the kinetics of mRNA and viral copy number following infection. (A, Top) The three-gene circuit at the heart of the lysis/lysogeny decision. (Bottom) The corresponding segment of the lambda genome. Upon viral entry,  $P_R$  expresses

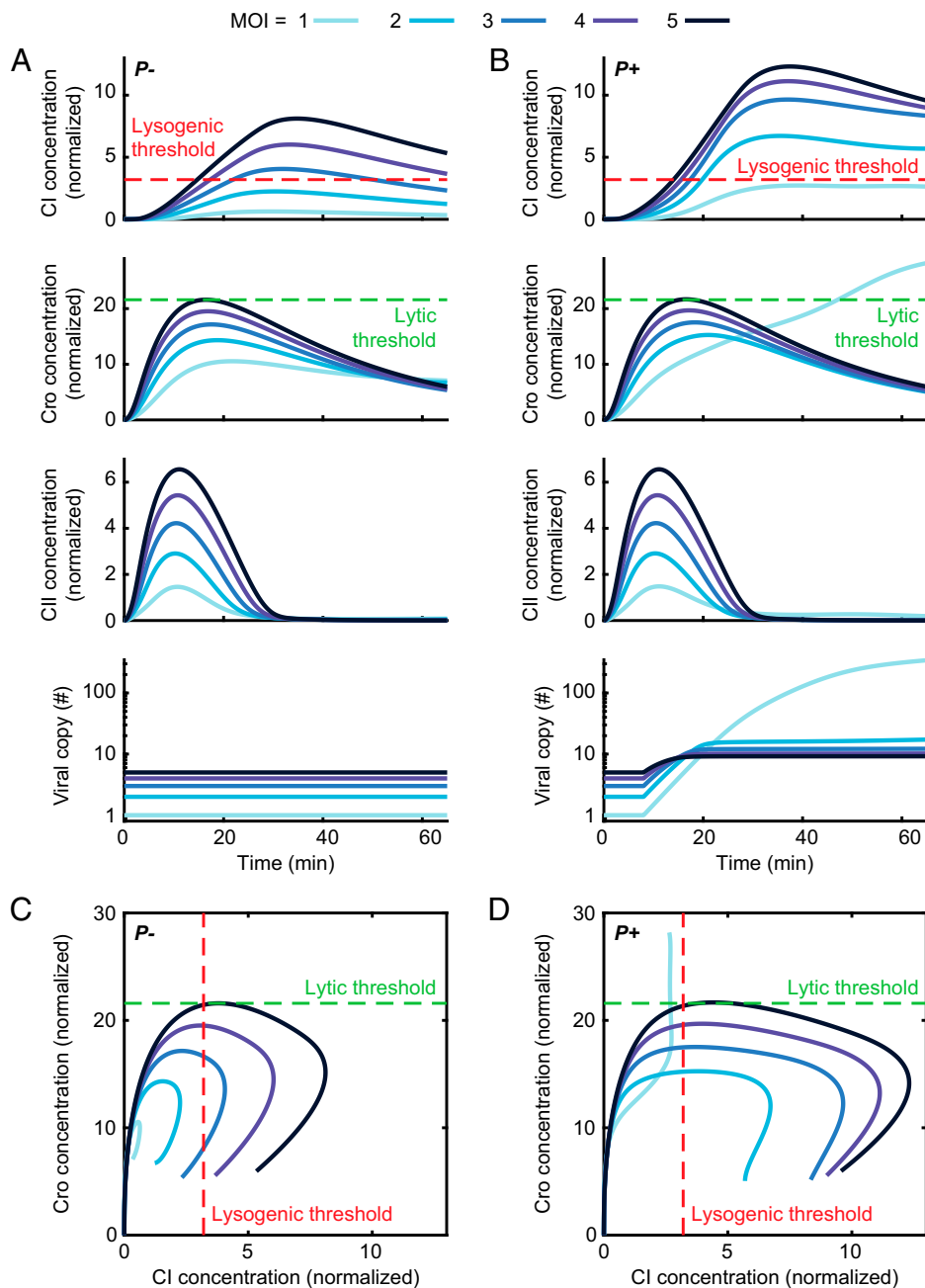
**Modeling Network Dynamics Reveals that a Lytic Decision Cannot Be Reached in the Absence of Viral Replication.**

The absence of clear MOI-driven changes in gene expression profiles following infection by a nonreplicating phage may indicate that divergence only takes place at the protein level, even if absent from the short-lived mRNA species. Alternatively, this absence may reflect a more fundamental point; namely, that viral replication is required for a lysis-to-lysogeny transition. To explore these possibilities, we constructed a deterministic mathematical model that describes the regulatory interactions between *cl*, *cro*, and *cII* as well as the coupling between gene expression and viral replication (Fig. 2A and SI Appendix, Theoretical Methods). Building on previous theoretical efforts (9, 19, 22), our model captures, phenomenologically, both direct interactions between the three genes (e.g., the activation of *cl* transcription from  $P_{RE}$  by CII and the repression of *cro* transcription from  $P_R$  by CI) and indirect ones mediated by players that are not modeled explicitly [e.g., CIII-mediated suppression of CII degradation (30)]. As its output, the model produces the population-averaged temporal dynamics of the viral copy number and mRNA and protein concentrations for a given initial MOI. To estimate the parameters governing gene regulation in the network, we fitted the model to the experimental mRNA kinetics during  $P^-$  infection by minimizing an objective function measuring the agreement between the two using particle swarm optimization (PSO) (31) (SI Appendix, Theoretical Methods). This procedure yielded a good agreement between the model and experiments (Fig. 2C and SI Appendix, Fig. S7) and allowed us to predict cellular variables that are not directly measurable in the experiments, such as protein concentrations and the activity of individual phage promoters.

To relate the gene expression dynamics computed by our model with the infection outcome, we assumed that cell fate is determined by whether Cro or CI concentration in the cell reaches a threshold value (16). The Cro threshold captures its multiple putative roles in establishing lysis: repressing *cl* transcription from  $P_{RM}$  and (indirectly, by repressing *cII* transcription from  $P_R$ ) from  $P_{RE}$  and the requirement that Q (encoded by the same transcript as Cro) reaches sufficient level to enable readthrough of the late lytic genes transcribed from  $P_R$  (17). As will be seen, our model suggests that it is the latter feature that sets the required Cro threshold. The lysogenic threshold, on the other hand, corresponds to CI levels sufficient to turn off the  $P_L$  and  $P_R$  promoters, thereby repressing the expression of lytic genes and phage replication (23).

Using our model to infer protein concentration dynamics following  $P^-$  infection, we found that, consistent with what we inferred from the mRNA data above, there is no obvious divergence in the trajectories. Cro, CI, and CII concentrations first rise and then decrease, with the maximal value reached by each protein increasing with MOI (Fig. 3A). As was the case with mRNA, this value is approximately linear for CI and sublinear

both *cro* and (following a leaky terminator) *cII*. CII then activates *cl* expression from  $P_{RE}$ . CI and Cro repress  $P_R$  and  $P_L$  as well as phage replication. In a lysogen, CI regulates its own expression from  $P_{RM}$ . (B) Images of a single *E. coli* cell at 10 min following infection by  $\lambda$  cI857 Pam80 P1parS. Phage genomes are labeled using ParB-parS and the mRNA for *cl*, *cro*, and *cII* using single-molecule fluorescence in situ hybridization. The yellow dashed line indicates the cell boundary. (C) The numbers of *cl*, *cro*, and *cII* mRNA per cell at different times following infection by  $P^-$  phage ( $\lambda$  cI857 Pam80 P1parS) at MOI = 1 to 5. Markers and error bars indicate experimental mean  $\pm$  SEM per sample (refer to SI Appendix, Table S6 for detailed sample sizes). Solid lines indicate model fit. (D) Viral copy number measured using qPCR following infection at MOI = 1 by  $P^+$  and  $P^-$  phages. Markers and error bars indicate experimental mean  $\pm$  SD because of qPCR calibration uncertainty. Lines indicate model fits. Refer to SI Appendix for detailed information.



**Fig. 3.** Phage replication is required for an MOI-driven lysis-to-lysogeny transition. (A) Model-predicted CI concentrations (normalized by threshold for CI repression of  $cro$  transcription), Cro concentrations (normalized by threshold for Cro repression of  $P_{RM}$ ), CII concentrations (normalized by threshold for CII activation of  $P_{RE}$ ), and viral copy number during the first 65 min following infection by  $P^-$  (nonreplicating) phage at varying MOI. (B) Same as A during  $P^+$  infection. (C) Trajectories in the CI-Cro phase plane for the scenarios in A. (D) Same as C during  $P^+$  infection. Refer to *SI Appendix* for detailed information.

(partially dose compensated) for Cro (*SI Appendix, Fig. S8*). Crucially, these dynamics are inconsistent with the requirement that cells reach a lytic decision threshold in Cro at low MOI but fail to reach it at higher MOI. In other words, no Cro threshold can be defined, which results in a lytic decision only below a critical MOI (*SI Appendix, Theoretical Methods*). In contrast, a range of CI thresholds that ensure lysogeny above some critical MOI can be defined (demonstrated by the dashed red line in Fig. 3A). Therefore, the inferred protein dynamics suggest that the lytic threshold is never reached during  $P^-$  infection and that, at low MOI, neither lysis nor lysogeny is selected (Fig. 3C). This interpretation is consistent with the

known absence of lysis following infection by  $P^-$  phages (22, 32) but suggests that this failure reflects the state of the decision circuit rather than merely a failure to execute the chosen lytic pathway, which was the implicit assumption in previous works (7, 16, 21).

To test the robustness of our prediction that infection at low MOI by a nonreplicating phage results in a failure to reach a decision, we employed an ensemble modeling approach (33–35). To this end, we supplemented the best-fit model used in Fig. 3 with an ensemble of models with distinct parameter values, obtained by repeating the PSO procedure (>100 times) using random starting seeds and selecting an ensemble of



44 parameter sets that produce objective functions within 4% of the best fit (*SI Appendix, Fig. S7 and Theoretical Methods*). As expected, some model parameters were well constrained, whereas others varied several folds between the different models within the ensemble (*SI Appendix, Table S7*). However, despite this variation, 100% of the models were consistent with the prediction by the best-fit model that, in the absence of viral replication, the maximal Cro concentration increases with MOI, and therefore, a low MOI lytic decision is not possible (*SI Appendix, Table S8*).

**Viral Replication Modifies Protein Dynamics and Enables an MOI-Dependent Lysis–Lysogeny Decision.** We next sought to evaluate what effect viral replication would have on the system's behavior. To calibrate the model parameters pertaining to lambda replication and its regulation, we used qPCR measurements of genome number kinetics from low MOI infection by a replicating ( $P+$ ) phage (Fig. 2D) as well as published data for  $cI$  and  $cII$  expression following infection with  $P+$  phages,  $cI-$ ,  $cro-$ , and  $cro-P-$  mutants (22) (*SI Appendix, Figs. S9 and S10*). The resulting model allowed us to predict the kinetics of CI and Cro concentrations trajectories following infection by replicating phages at various MOIs (Fig. 3B).

Comparing these dynamics (Fig. 3B) to what we found for a nonreplicating phage (Fig. 3A), we find the CI's behavior is qualitatively similar, with a transient peak whose magnitude is again nearly linear with MOI (*SI Appendix, Fig. S8*), albeit higher in the presence of viral replication. Cro dynamics, in contrast, now exhibit a clear divergence between low and higher MOI, very unlike what was seen in the nonreplicating phage. Specifically, for MOI > 1, Cro levels in  $P+$  phage are hardly affected by replication and remain very similar to  $P-$ . However, for MOI = 1, Cro continuously increases during the time simulated (65 min), eventually exceeding the maximal level reached at higher MOIs. The divergence between low and high MOI is also observed in the dynamics of viral copy number (Fig. 3B): replication is suppressed at early ~20 min postinfection for MOI > 1 but continues throughout the simulation for MOI = 1.

The qualitative differences in behavior between  $P-$  and  $P+$  phages are further illustrated by examining the trajectories in the plane of Cro and CI concentrations (Fig. 3C and D). For nonreplicating phages, the trajectories for different MOIs are similar in shape and simply scale with MOI (Fig. 3C and *SI Appendix, Fig. S8*). For replicating phage, in contrast, trajectories clearly diverge between MOI = 1 and higher MOIs and, in particular, support a transition from lysis (Cro threshold crossing) to lysogeny (CI threshold crossing) with increasing MOI (Fig. 3D). Moreover, a single choice of thresholds is simultaneously consistent with the experimental phenotypes of both  $P-$  and  $P+$  phages in terms of the MOI value at which the transition to lysogeny occurs (~3 to 4 and 2 for  $P-$  and  $P+$  respectively; *SI Appendix, Theoretical Methods* and see Fig. 6D) (10). Notably, these predictions are robustly observed for the whole ensemble of fitted models. For replicating phage, all models show 1) a divergence of trajectories between MOI = 1 and higher MOI and 2) a lower minimal MOI required for crossing the lysogeny thresholds as compared to nonreplicating phages (*SI Appendix, Table S8*).

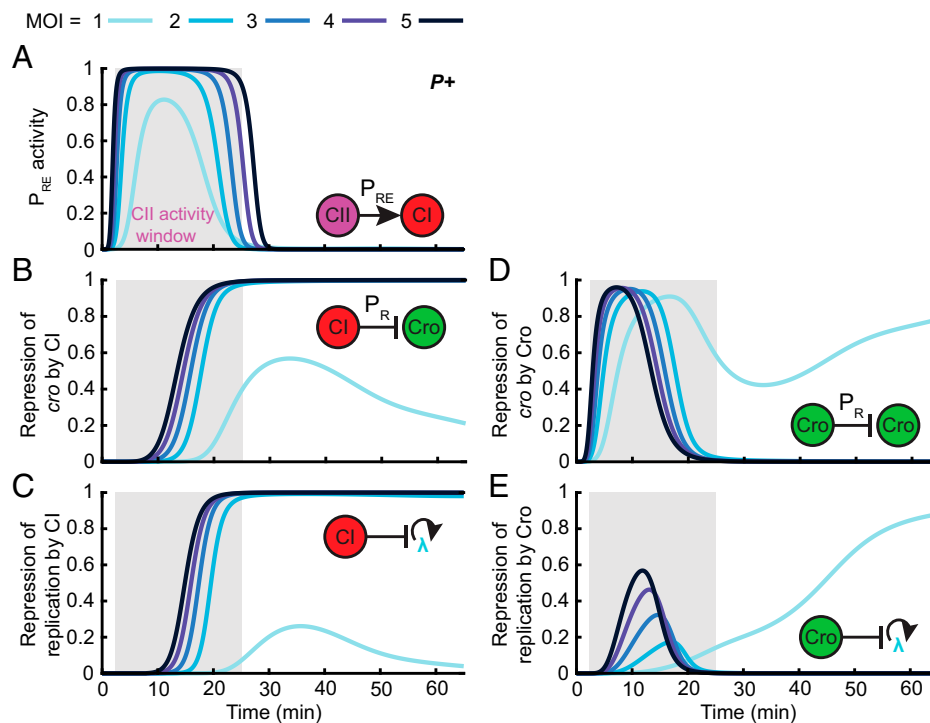
**CII Activation of  $P_{RE}$  Defines a Time Window for the Network's Response to MOI.** Having successfully recapitulated the decision phenotype, we next sought to understand how lambda reliably responds to the initial MOI even in the presence of viral replication. Since establishing lysogeny requires reaching a critical CI concentration, we focused on the response of  $cI$  expression to MOI. Two lambda promoters drive  $cI$  transcription,  $P_{RE}$  (activated by CII) and  $P_{RM}$  (autoregulated by CI) (23).  $P_{RM}$  is solely responsible for CI production in a lysogen (23), but

whether it plays a role during the initial decision has remained unresolved (36). Our model indicates that the MOI-driven increase in CI is caused by transcription from  $P_{RE}$ , and removing  $cI$  autoregulation does not eliminate that response (*SI Appendix, Fig. S11*). Analyzing the whole ensemble of fitted models, we confirmed that the MOI-dependent transition to lysogeny requires  $cI$  transcription from  $P_{RE}$  but not  $P_{RM}$  (*SI Appendix, Table S8*). This finding is consistent with reports that a wide range of mutations in  $P_{RM}$  permit the establishment of lysogeny (37, 38), whereas mutating  $P_{RE}$  or CII prevents it (23). The lower translation rate of CI from  $P_{RM}$  versus  $P_{RE}$  transcripts (a feature not modeled here) is expected to further diminish  $P_{RM}$ 's role. Thus, to elucidate CI's response to MOI, we focused on characterizing the CII-activated expression of  $cI$  during infection.

Our model indicates that CII-activated  $P_{RE}$  expression occurs in a single pulse, taking place within the first ~30 min of infection (Fig. 4A). The amplitude (per phage) and duration of this  $P_{RE}$  activation pulse depend only weakly on MOI (Fig. 4A and *SI Appendix, Fig. S12*), reflecting the fact that CII reaches its  $P_{RE}$  activation threshold at all MOIs (Fig. 3A and B). These predictions contrast with previous suggestions of an ultrasensitive increase in  $cI$  transcription with MOI (17, 20) but are robustly observed in our ensemble of fitted models (*SI Appendix, Table S8*). Notably, these model predictions are supported by direct measurements of nascent  $cI$  mRNA level at individual phage genomes (*SI Appendix, Fig. S13*) and are also consistent with our findings that, in nonreplicating phages, cellular  $cII$  numbers are dosage compensated, whereas  $cI$  level scales linearly with MOI (*SI Appendix, Fig. S6*). The MOI independence of  $cI$  expression from individual viral copies during  $P_{RE}$  activation explains the approximately linear scaling of cellular CI concentration with increasing MOI (Fig. 3B and *SI Appendix, Fig. S8*). This scaling nevertheless satisfies a necessary condition for the lysogeny decision by allowing the maximal CI concentration at MOI  $\geq 2$  to reach the critical level sufficient to repress both  $cro$  expression (Fig. 4B) and viral replication (Fig. 4C). This repression is established during the  $P_{RE}$  activation window and persists throughout infection leading to lysogeny.

As for Cro, the divergence of its dynamics between low and high MOI manifests itself in qualitative changes in its ability to repress  $P_R$  and viral replication (Fig. 4D and E). Cro's role in regulating viral replication during the decision appears minor relative to CI (Fig. 4C), becoming dominant only at later stages of lytic development at MOI = 1 (Fig. 4E). However, early in the  $P_{RE}$  expression window, Cro does play an important role in repressing  $P_R$ , and thereby CII, at all MOIs, to ensure the closing of the CII activity window. Notably, for MOI = 1, Cro continues to play a role in repressing  $P_R$  transcription at later times, as CI levels are insufficient to keep it fully repressed (Fig. 4B and D).

The results above pinpoint key features of the decision network that must be in place to enable an MOI-dependent choice—activation of  $P_{RE}$  by CII, repression of  $P_R$  by Cro, and repression of replication and  $cro$  expression by CI. Perturbations to our ensemble of models, which eliminate these interactions, destroy the lysis-to-lysogeny transition (*SI Appendix, Table S9*). In addition, ensemble perturbations predict two other features that are necessary for the existence of the MOI-insensitive time window: high cooperativity of CII activation of  $P_{RE}$  and rapid CII degradation (*SI Appendix, Table S9*). In contrast, repression of viral replication of Cro plays a major role in only some of the parameter sets within the ensemble (*SI Appendix, Table S9*) and may therefore be a redundant mechanism, increasing the robustness of the decision (39).



**Fig. 4.** CII activation of  $P_{RE}$  defines a time window for the network's response to MOI. (A) Model-predicted  $P_{RE}$  promoter activity (per phage) following infection by  $P_+$  phage at MOI = 1 to 5. Gray shading indicates the MOI-averaged CII activity window defined as the period during which  $P_{RE}$  activity is greater than 10% of its maximum. (B) The strength of *cro* repression by CI calculated as the magnitude of the CI repression term in the  $P_R$  transcription rate following infection by  $P_+$  phage at MOI = 1 to 5. (C) The strength of repression of replication by CI calculated as the magnitude of the CI repression term in the viral replication rate following infection by  $P_+$  phage at MOI = 1 to 5. (D) The strength of *cro* repression by Cro calculated analogously to the term in B. (E) The strength of repression of replication by Cro calculated analogously to the term in D. Refer to *SI Appendix* for detailed information.

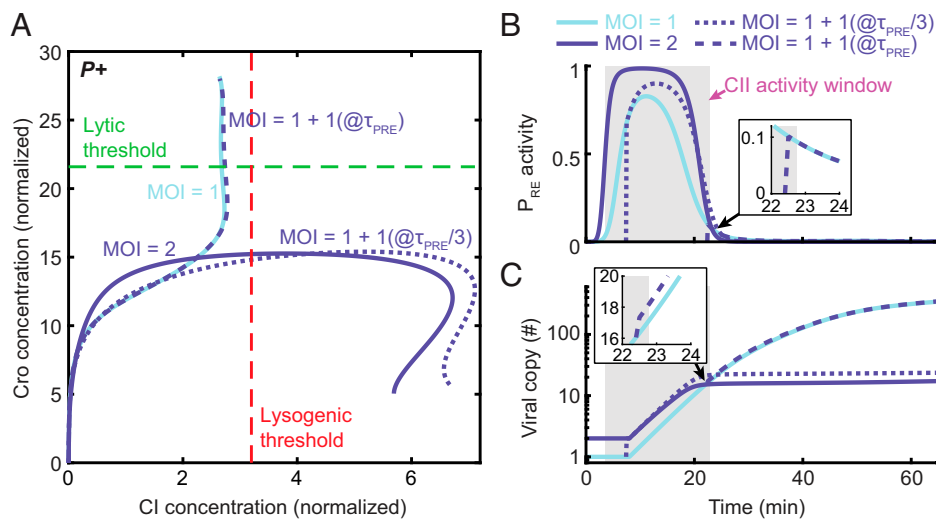
Finally, examination of the system's dynamics during the CII activity window provides a mechanistic insight for defining the lytic Cro threshold: this threshold is unlikely to reflect the repression of  $P_{RM}$  (which is unnecessary for the decision, *SI Appendix, Fig. S11*) or of  $P_R$  (which takes place for all MOIs, Fig. 4D). Accordingly, in our ensemble, the regulatory thresholds for these processes lie considerably below the lytic decision threshold (*SI Appendix, Table S10*). While the Cro threshold for repressing viral replication is of the same order as the lytic threshold, this repression is not needed in the majority of ensemble models (*SI Appendix, Table S9*). These observations suggest that the lytic threshold serves as a proxy for the accumulation of sufficient Q protein to enable readthrough of the late lytic genes transcribed from  $P_R$  (17).

**Changes in Viral Copy Number Outside the CII Activity Window Do Not Alter the Decision.** The findings in the preceding section reveal how CI levels—and the propensity to lysogenize—increase with MOI. However, a reliable MOI-based decision also requires that viral replication inside the cell will not obfuscate the initial response to MOI. We reasoned that, for this to hold, the system should become insensitive to changes in viral dosage once the window for CII activation of  $P_{RE}$  is closed. To test this hypothesis, we followed the approach of Cortes et al. (20) and used the model to examine what happens in the case of delayed infection. Specifically, we modeled an infection by a single phage followed by a second single-phage infection at time  $\tau_d$  later (Fig. 5). We found that, indeed, if the second infection takes place after the end of the CII activity window  $\tau_{PRE}$ , the outcome is lysis, and the CI and Cro trajectories are indistinguishable from those at MOI = 1 (Fig. 5A). If, in contrast, the delayed infection occurs early enough within the CII activity window, and the infection results in lysogeny, with CI and Cro trajectories similar to those for a

synchronized infection at MOI = 2 (Fig. 5A). Infecting with higher numbers of late-arriving viruses prolongs the time window in which the late phages can affect the decision but not beyond  $\tau_{PRE}$  (*SI Appendix, Fig. S14*). Thus, the infection outcome is insensitive to changes in viral copy number that take place outside the time window determined by CII activity. This prediction robustly holds across all models of the ensemble (*SI Appendix, Table S8*).

Why does delayed infection result in a diminished response? Our model indicates reduced  $P_{RE}$  expression from the second virus since that virus is not present for the entire duration of the CII activity pulse (Fig. 5B). This results in lower cellular accumulation of CI during that time window as compared to simultaneous coinfection (Fig. 5A). Furthermore, the delay impacts not only the late-infecting virus itself but also all viruses produced subsequently through viral replication (Fig. 5C). We note that, through the combination of Cro repression of  $P_R$  and active CII degradation (23), the decision network constrains CII activity to a single time window. Subsequent changes in viral copy number after the initial infection cannot overcome this constraint. These features of the system's response to delayed infection can also explain why rampant viral replication during infection at MOI = 1 does not cause a switch to lysogeny: While replication generates >100 additional genome copies (Fig. 2D), viruses produced outside the CII activity window are unable to express *cI* from  $P_{RE}$  (*SI Appendix, Fig. S15*). The opportunity to “flip” the decision switch has already been lost.

**Phage Replication Enables the Lytic Choice and Lowers the MOI Required for Lysogeny.** We have thus seen how phage replication is tolerated, that is, how a reliable response to the initial MOI is achieved despite the subsequent change in viral copy number. Recall, however, that comparing CI–Cro trajectories



**Fig. 5.** Changes in viral copy number outside the CII activity window do not alter the decision. (A) Model-predicted system trajectories in the plane of Cro and CI concentrations (normalized as in Fig. 3) during the first 65 min following infection by  $P^+$  phages at four different scenarios: infection by a single phage (solid line, light blue), infection by a single phage followed by a second phage at time  $\tau_{PRE}/3$  (with  $\tau_{PRE}$  the end of the CII activity window at  $MOI = 1$ ; dotted line, dark blue) and  $\tau_{PRE}$  (dashed line, dark blue), and simultaneous infection by two phages (solid line, dark blue). (B)  $P_{RE}$  activity from the second arriving phages for the cases modeled in A. The shaded gray region indicates the CII activity window at  $MOI = 1$ . (Inset) Infection by a second phage at time  $\tau_{PRE}$ . (C) Viral copy number over time for the cases modeled in A. (Inset) Infection by a second phage at time  $\tau_{PRE}$ . Refer to [SI Appendix](#) for detailed information.

in replicating (Fig. 3D) and nonreplicating (Fig. 3C) phages indicated that viral replication is not only tolerated but, in fact, required for the existence of an MOI-dependent lysis-to-lysogeny transition. To understand why that is the case, we first addressed the absence of a lytic choice following  $P^-$  infection at  $MOI = 1$ . Our model indicates that, in both  $P^+$  and  $P^-$ ,  $cro$  transcription from  $P_R$  (per phage) is repressed greater than twofold within  $\sim 10$  min of infection (Fig. 6A and [SI Appendix, Fig. S16](#) depicts the corresponding experimental data). However, the presence of additional gene copies in the  $P^+$  case results in higher Cro concentration later in the infection, sufficient to cross the lytic threshold (Fig. 6B). Viral replication thus serves to boost total Cro expression despite repression of its transcription at the individual phage level.

As for the effect of replication on the lysogenic choice, we find that  $cI$  transcription from  $P_{RE}$  during  $P^-$  infection follows a similar pattern to  $P^+$ , namely, a single pulse whose duration and amplitude per phage depend only weakly on MOI ([SI Appendix, Fig. S17](#); compare to Fig. 4A and [SI Appendix, Fig. S12](#)). However, as in the case of Cro, the presence of added gene copies during  $P^+$  infection leads to considerably higher CI accumulation than for  $P^-$  (Fig. 6C). Consequently, while replicating phages reach the lysogenic CI threshold at  $MOI = 2$ , nonreplicating ones require a higher MOI to reach that threshold and establish lysogeny. The theoretical prediction that  $P^-$  phage lysogenizes at higher MOI than  $P^+$  is consistently observed across the ensemble of fitted models ([SI Appendix, Table S8](#)) and is borne out in experiments (10) (Fig. 6D).

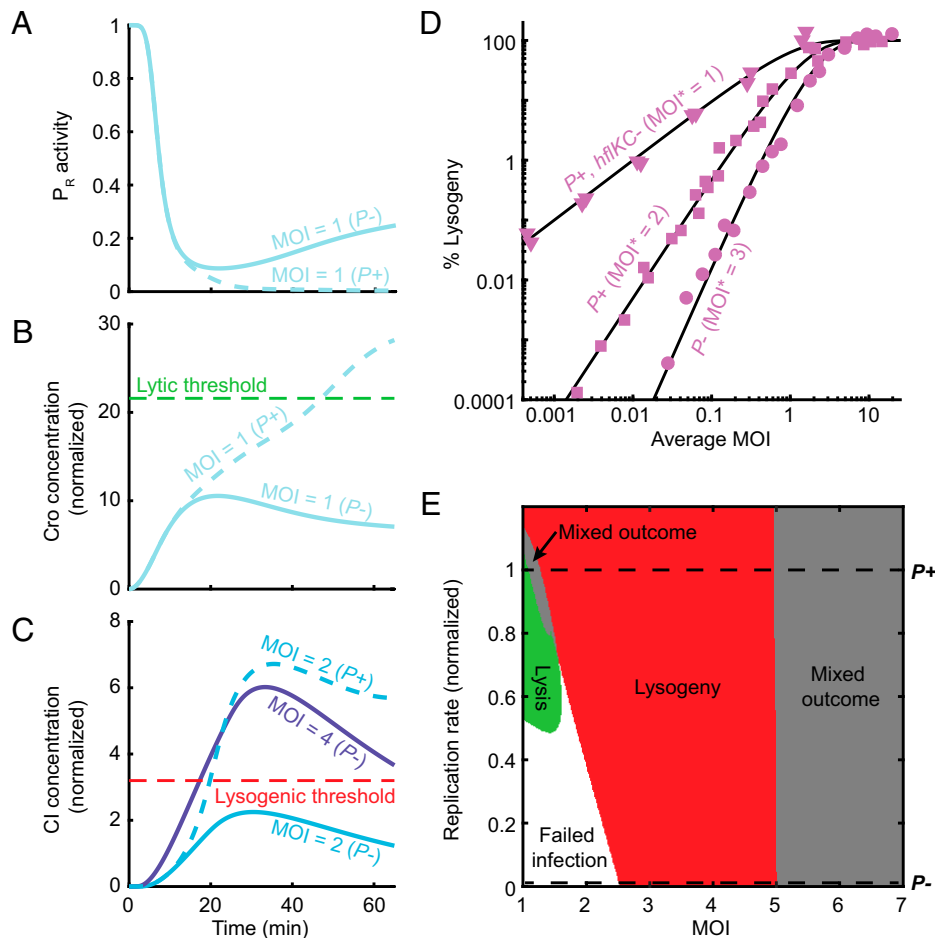
To generalize the effect of viral replication on the lysis/lysogeny decision, we simulated infections at MOI in the range 1 to 7 while varying the phage replication rate from zero to  $1.5\times$  that of  $P^+$  phage. Determining the infection outcome at each MOI and replication rate yielded the two-dimensional “fate diagram” shown in Fig. 6E. Consistent with the preceding discussion, we find that both the existence of a lytic outcome and the minimal MOI at which the transition to lysogeny occurs depend on the viral replication rate. The ability to replicate is not by itself sufficient to enable the lytic pathway. Rather, there is a minimum required replication rate below which  $MOI = 1$  infections fail to achieve either outcome. As for lysogeny, the

MOI at which this fate is chosen decreases with the viral replication rate (Fig. 6E). When replication is sufficiently rapid, the model predicts a lysogenic outcome even at  $MOI = 1$  (Fig. 6E and [SI Appendix, Table S9](#)). While we are unaware of an experimental test for this prediction, we note that the model predicts a similar behavior when the CII activity window is extended by inhibition of CII degradation ([SI Appendix, Fig. S18](#) and [Table S9](#)), a result validated by experiments (30) (Fig. 6D).

Interestingly, there are two regions where the system’s trajectories cross both the lytic and lysogenic thresholds in the course of infection (Fig. 6E). The first of those occurs at high replication rates in the MOI range between lysis and lysogeny. We are uncertain how to interpret this feature, but it is intriguing to note that, at the single-cell level, it may correspond to the range of infection parameters in which stochastic effects become important, and consequently, individual cells exhibit different fates as reported experimentally (11, 12, 40). The analysis of cellular heterogeneity is outside the premise of our current model, which captures the population-averaged behavior only. A second region where mixed outcomes are predicted is found for  $MOI \geq 5$  and may correspond to a scenario in which the overexpression of viral proteins results in the halting of cell growth rather than a lytic or lysogenic outcome, consistent with experimental data (12).

## Discussion

The combination of single-molecule genome and mRNA measurement in individual cells with theoretical modeling provided us with insights into the way lambda counts coinfecting phages to bias the lysis–lysogeny decision. Early theoretical studies of the postinfection decision sought insight to the phage’s binary choice in the toggle switch comprised of the mutually antagonistic CI and Cro, which governs lysogenic maintenance and lytic induction (9, 19, 41, 42). This famous “genetic switch” exhibits bistability (43) with well-defined states characterized by high CI (lysogeny) and high Cro (lytic onset), respectively. These features, and the tremendous body of experimental and theoretical knowledge that has accrued about the pairwise CI/Cro interactions (14, 18), explain the focus on this element as



**Fig. 6.** Replication is required for the lytic outcome and lowers the MOI required for lysogeny. (A) Model-predicted  $P_R$  activity per phage during  $P_-$  (solid blue line) and  $P_+$  (dashed blue line) infection at MOI = 1. (B) Cellular Cro concentration (normalized as in Fig. 3) for the cases modeled in A. (C) Cellular CI concentration (normalized as in Fig. 3) during  $P_-$  infection at MOI = 2 and 4 (solid light and dark blue lines, respectively) and during  $P_+$  infection at MOI = 2 (dashed line). (D) The fraction of cells undergoing lysogeny as a function of average MOI during bulk infection with  $P_-$  (circles),  $P_+$  (squares), and phages with prolonged CII lifetime ( $P_+$  phages infecting  $hflKC^-$  hosts; triangles). The experimental data were normalized and fitted to a model (black lines) in which virus-cell encounters follow Poisson statistics, and infection at MOI  $\geq$  MOI\* results in lysogeny (10) as described in *SI Appendix*. The  $hflKC^-$  strains are either  $\Delta hflK$  or  $\Delta hflC$  (*SI Appendix*, Table S1). (E) Predicted infection outcome as a function of MOI and viral replication rate (normalized by the fitted replication rate of  $P_+$  phage). Refer to *SI Appendix* for detailed information.

the key to the decision. Moreover, theoretical work has shown that MOI could indeed drive a bifurcation of the CI/Cro switch's steady state, consistent with a transition from lysis to lysogeny (9, 19). Our analysis, however, suggests that this is not how the lambda decision unfolds. Instead, each phage initially attempts to execute a preset pattern of gene expression independent of the MOI. In this cascade of events, *ci* transcription takes place predominantly through the transient activation of  $P_{RE}$  by CII, while *ci* autoregulatory expression from  $P_{RM}$  is unnecessary. The resulting cellular CI expression is approximately linear in MOI, indicating the absence of an ultrasensitive response to CII as previously suggested (17, 20, 44). This linearity holds despite the high Hill coefficient of  $P_{RE}$  activation because even a single phage produces enough CII to activate  $P_{RE}$ . Given the fixed gene expression cascade at the individual phage level, it is the introduction of time-varying gene dosage due to viral replication—rather than the standalone topology of the viral circuit—that enables the subsequent divergence of gene expression trajectories and cell-fate choices at low and high MOI.

The time-varying viral copy number is found to be critical for both possible outcomes of infection. The choice of lysogeny depends on the number of lambda copies present during the

early decision window, set by CII activation of  $P_{RE}$  (Fig. 4A). The finite response window immunizes the lambda decision to changes in viral copy number that take place outside it, thus allowing reliable detection of the initial MOI. However, the role of viral copy number does not end then and is, in fact, crucial for reaching the protein threshold required for establishing either fate: Cro for lysis or CI for lysogeny. Cro (and by proxy, the lytic activator Q) continues to accumulate through late infection, reaching the lytic decision threshold  $\sim$ 50 min postinfection (Fig. 6B). Cro's continued accumulation is driven by late viral replication, despite the repression of  $P_R$  at the single-phage level (Fig. 6A). As for lysogeny, while this fate is achievable in the absence of viral replication, it is replication that ensures that coinfection by more than one phage is sufficient to drive lysogeny; in the absence of replication, CI accumulates insufficiently, and higher MOI is required to reach the lysogenic threshold (Fig. 6C).

Our ensemble modeling approach enables us to pinpoint the critical regulatory interactions and their parametric regimes, which underlie the formation of the MOI response window and subsequent cell-fate decision (*SI Appendix*, Table S9 and Figs. S19 and S20). Fast initial accumulation of CII past its  $P_{RE}$  activation threshold makes CI concentration linearly scale with the



viral dosage, whereas Cro autorepression makes its concentration partially dosage compensated. Repression of  $P_R$  by Cro, fast degradation of CII, and cooperativity of  $P_{RE}$  activation together lead to the closing of the time window at all MOIs. If enough CI to keep  $P_R$  and viral replication repressed has accumulated during that time, cells follow the lysogenic pathway. Otherwise, continued viral replication overrides the per-copy repression of *cro* and leads to sufficient Cro (and Q) accumulation to trigger lysis.

The ensemble modeling also leads to several robust predictions (SI Appendix, Table S8). Some of those provide interpretations for previous observations. For example, the failure to lyse following infection by  $P^-$  phage at low MOI (22, 32) is explained by the inability of Cro (as a proxy for Q) to reach the lytic threshold. And the increase in minimal MOI required for lysogeny in  $P^-$  versus  $P^+$  phages (Fig. 6D) (10, 22) is found to reflect faster accumulation of CI due to replication-driven increase in gene dosage. Other predictions will await future experimental validation. For instance, the existence of a finite (~20 to 30 min) window during which an increase in viral gene dosage via reinfection or replication can affect cell-fate decisions, or the strong effect that perturbing viral replication rate is predicted to have on the lysis/lysogeny decision.

The relation between gene dosage and the output of genetic networks has been explored in diverse biological contexts, both natural (45–47) and synthetic (48–51). In some instances, changes in gene copy number were found to have a significant effect on phenotype (52–54), whereas in other cases, mechanisms of dosage compensation buffer the network output from such changes (51, 55–58). The lambda decision exhibits a

richness of dosage response beyond what was previously documented, with the transcriptional output either linear in dosage or partially compensating it, for different genes in the network at different times during the infection. Consequently, viral replication is found to facilitate rather than hinder the implementation of a reliable decision. Since cellular decisions frequently take place even as gene copy number is changing (59–61), this inextricable coupling of gene dosage and network output cannot be ignored if one aims for a predictive description of cellular decision making.

## Materials and Methods

All bacterial and phage strains, experimental procedures, microscopy, data analysis, and theoretical modeling used in this study are described in SI Appendix.

**Data Availability.** Bacterial and phage strains are available upon request. All simulation codes can be found in Zenodo: <https://doi.org/10.5281/zenodo.5639007>. Previously published data were used for this work (22).

**ACKNOWLEDGMENTS.** We are grateful to the following people for their generous advice and for providing reagents: R. Arbel-Goren, S. Austin, G. Balázs, M. Cortes, I. Dodd, M. Feiss, J. Harris, C. Hayter, C. Herman, K. Shearwin, J. Stavans, F. St-Pierre, L. Thomason, G. Vasen, J. Weitz, L. Weinberger, Z. Yu, L. Zeng, and all members of the I.G. and O.A.I. groups. This work was supported by the NSF Center for Theoretical Biological Physics (NSF PHY-2019745) and Grant PHY-1522550. The work was supported in part by the Big-Data Private-Cloud Research Cyberinfrastructure MRI Award funded by the NSF under Grant CNS-1338099 and by Rice University. The work in the I.G. laboratory is supported by the NIH Grant R35 GM140709 and the NSF Grant PHY 1430124 (PFC: Center for the Physics of Living Cells). O.A.I. also acknowledges support by the Welch Foundation Grant C-1995 and the NSF Grant MCB-1616755.

- G. Ofir, R. Sorek, Contemporary phage biology: From classic models to new insights. *Cell* **172**, 1260–1270 (2018).
- I. Golding, S. Coleman, T. V. P. Nguyen, T. Yao, “Decision making by temperate phages” in *Encyclopedia of Virology*, D. H. Bamford, M. Zuckerman, Eds. (Academic Press, Cambridge, MA, 2021), pp. 88–97.
- R. B. Bourret, M. S. Fox, Lysogenization of *Escherichia coli* him+, himA, and himD hosts by bacteriophage Mu. *J. Bacteriol.* **170**, 1672–1682 (1988).
- M. Levine, Mutations in the temperate phage P22 and lysogeny in *Salmonella*. *Virology* **3**, 22–41 (1957).
- Z. Erez *et al.*, Communication between viruses guides lysis-lysogeny decisions. *Nature* **541**, 488–493 (2017).
- J. E. Silpe, B. L. Bassler, A host-produced quorum-sensing autoinducer controls a phage lysis-lysogeny decision. *Cell* **176**, 268–280.e13 (2019).
- A. Arkin, J. Ross, H. H. McAdams, Stochastic kinetic analysis of developmental pathway bifurcation in phage lambda-infected *Escherichia coli* cells. *Genetics* **149**, 1633–1648 (1998).
- I. Golding, Decision making in living cells: Lessons from a simple system. *Annu. Rev. Biophys.* **40**, 63–80 (2011).
- J. S. Weitz, Y. Milevko, R. I. Joh, E. O. Voit, Collective decision making in bacterial viruses. *Biophys. J.* **95**, 2673–2680 (2008).
- P. Kourilsky, Lysogenization by bacteriophage lambda. I. Multiple infection and the lysogenic response. *Mol. Gen. Genet.* **122**, 183–195 (1973).
- M. Lieb, The establishment of lysogenicity in *Escherichia coli*. *J. Bacteriol.* **65**, 642–651 (1953).
- L. Zeng *et al.*, Decision making at a subcellular level determines the outcome of bacteriophage infection. *Cell* **141**, 682–691 (2010).
- S. R. Casjens, R. W. Hendrix, Bacteriophage lambda: Early pioneer and still relevant. *Virology* **479–480**, 310–330 (2015).
- D. L. Court, A. B. Oppenheim, S. L. Adhya, A new look at bacteriophage lambda genetic networks. *J. Bacteriol.* **189**, 298–304 (2007).
- I. B. Dodd, K. E. Shearwin, J. B. Egan, Revisited gene regulation in bacteriophage lambda. *Curr. Opin. Genet. Dev.* **15**, 145–152 (2005).
- R. I. Joh, J. S. Weitz, To lyse or not to lyse: Transient-mediated stochastic fate determination in cells infected by bacteriophages. *PLoS Comput. Biol.* **7**, e1002006 (2011).
- O. Kobiler *et al.*, Quantitative kinetic analysis of the bacteriophage lambda genetic network. *Proc. Natl. Acad. Sci. U.S.A.* **102**, 4470–4475 (2005).
- M. Ptashne, *A Genetic Switch: Phage Lambda Revisited* (Cold Spring Harbor Laboratory Press, Cold Spring Harbor, NY, ed. 3, 2004).
- M. Avlund, I. B. Dodd, K. Sneppen, S. Krishna, Minimal gene regulatory circuits that can count like bacteriophage lambda. *J. Mol. Biol.* **394**, 681–693 (2009).
- M. G. Cortes, J. T. Trinh, L. Zeng, G. Balázs, Late-arriving signals contribute less to cell-fate decisions. *Biophys. J.* **113**, 2110–2120 (2017).
- H. H. McAdams, L. Shapiro, Circuit simulation of genetic networks. *Science* **269**, 650–656 (1995).
- Q. Shao *et al.*, Coupling of DNA replication and negative feedback controls gene expression for cell-fate decisions. *iScience* **6**, 1–12 (2018).
- A. B. Oppenheim, O. Kobiler, J. Stavans, D. L. Court, S. Adhya, Switches in bacteriophage lambda development. *Annu. Rev. Genet.* **39**, 409–429 (2005).
- S. Gandon, Why be temperate: Lessons from bacteriophage lambda. *Trends Microbiol.* **24**, 356–365 (2016).
- V. Sinha, A. Goyal, S. L. Svenningsen, S. Semsey, S. Krishna, *In silico* evolution of lysis-lysogeny strategies reproduces observed lysogeny propensities in temperate bacteriophages. *Front. Microbiol.* **8**, 1386 (2017).
- M. Wang, J. Zhang, H. Xu, I. Golding, Measuring transcription at a single gene copy reveals hidden drivers of bacterial individuality. *Nat. Microbiol.* **4**, 2118–2127 (2019).
- A. Tal, R. Arbel-Goren, N. Costantino, D. L. Court, J. Stavans, Location of the unique integration site on an *Escherichia coli* chromosome by bacteriophage lambda DNA in vivo. *Proc. Natl. Acad. Sci. U.S.A.* **111**, 7308–7312 (2014).
- B. Youngren, H. J. Nielsen, S. Jun, S. Austin, The multifork *Escherichia coli* chromosome is a self-duplicating and self-segregating thermodynamic ring polymer. *Genes Dev.* **28**, 71–84 (2014).
- S. O. Skinner, L. A. Sepúlveda, H. Xu, I. Golding, Measuring mRNA copy number in individual *Escherichia coli* cells using single-molecule fluorescent in situ hybridization. *Nat. Protoc.* **8**, 1100–1113 (2013).
- O. Kobiler, A. Rokney, A. B. Oppenheim, Phage lambda CIII: A protease inhibitor regulating the lysis-lysogeny decision. *PLoS One* **2**, e363 (2007).
- J. Kennedy, R. Eberhart, “Particle swarm optimization” in *Proceedings of ICNN’95 - International Conference on Neural Networks* (ICNN, Perth, Australia, 1995), pp. 1942–1948.
- K. Brooks, Studies in the physiological genetics of some suppressor-sensitive mutants of bacteriophage lambda. *Virology* **26**, 489–499 (1965).
- L. Kuepfer, M. Peter, U. Sauer, J. Stelling, Ensemble modeling for analysis of cell signaling dynamics. *Nat. Biotechnol.* **25**, 1001–1006 (2007).
- G. L. Medlock, J. A. Papin, Guiding the refinement of biochemical knowledgebases with ensembles of metabolic networks and machine learning. *Cell Syst.* **10**, 109–119.e3 (2020).
- S. M. Ud-Dean, R. Gunawan, Ensemble inference and inferability of gene regulatory networks. *PLoS One* **9**, e103812 (2014).
- C. B. Michalowski, J. W. Little, Positive autoregulation of *ci* is a dispensable feature of the phage lambda gene regulatory circuitry. *J. Bacteriol.* **187**, 6430–6442 (2005).
- C. B. Michalowski, M. D. Short, J. W. Little, Sequence tolerance of the phage lambda PRM promoter: Implications for evolution of gene regulatory circuitry. *J. Bacteriol.* **186**, 7988–7999 (2004).

38. R. A. Schubert, I. B. Dodd, J. B. Egan, K. E. Shearwin, Cro's role in the CI Cro bistable switch is critical for lambda's transition from lysogeny to lytic development. *Genes Dev.* **21**, 2461–2472 (2007).
39. H. Kitano, Biological robustness. *Nat. Rev. Genet.* **5**, 826–837 (2004).
40. F. St-Pierre, D. Endy, Determination of cell fate selection during phage lambda infection. *Proc. Natl. Acad. Sci. U.S.A.* **105**, 20705–20710 (2008).
41. J. Reinitz, J. R. Vaisnys, Theoretical and experimental analysis of the phage lambda genetic switch implies missing levels of co-operativity. *J. Theor. Biol.* **145**, 295–318 (1990).
42. M. A. Shea, G. K. Ackers, The OR control system of bacteriophage lambda. A physical-chemical model for gene regulation. *J. Mol. Biol.* **181**, 211–230 (1985).
43. M. Bednarz, J. A. Halliday, C. Herman, I. Golding, Revisiting bistability in the lysis/lysogeny circuit of bacteriophage lambda. *PLoS One* **9**, e100876 (2014).
44. J. Vohradsky, Neural model of the genetic network. *J. Biol. Chem.* **276**, 36168–36173 (2001).
45. M. Guo, D. Davis, J. A. Birchler, Dosage effects on gene expression in a maize ploidy series. *Genetics* **142**, 1349–1355 (1996).
46. J. Narula *et al.*, Chromosomal arrangement of phosphorelay genes couples sporulation and DNA replication. *Cell* **162**, 328–337 (2015).
47. J. R. Pollack *et al.*, Microarray analysis reveals a major direct role of DNA copy number alteration in the transcriptional program of human breast tumors. *Proc. Natl. Acad. Sci. U.S.A.* **99**, 12963–12968 (2002).
48. L. Baumgart, W. Mather, J. Hasty, Synchronized DNA cycling across a bacterial population. *Nat. Genet.* **49**, 1282–1285 (2017).
49. A. Becskei, L. Serrano, Engineering stability in gene networks by autoregulation. *Nature* **405**, 590–593 (2000).
50. L. Bleris *et al.*, Synthetic incoherent feedforward circuits show adaptation to the amount of their genetic template. *Mol. Syst. Biol.* **7**, 519 (2011).
51. J. Yang *et al.*, A synthetic circuit for buffering gene dosage variation between individual mammalian cells. *Nat. Commun.* **12**, 4132 (2021).
52. D. E. Cook *et al.*, Copy number variation of multiple genes at Rhg1 mediates nematode resistance in soybean. *Science* **338**, 1206–1209 (2012).
53. L. G. Maron *et al.*, Aluminum tolerance in maize is associated with higher MATE1 gene copy number. *Proc. Natl. Acad. Sci. U.S.A.* **110**, 5241–5246 (2013).
54. D. Wright *et al.*, Copy number variation in intron 1 of SOX5 causes the Pea-comb phenotype in chickens. *PLoS Genet.* **5**, e1000512 (2009).
55. M. Acar, B. F. Pando, F. H. Arnold, M. B. Elowitz, A. van Oudenaarden, A general mechanism for network-dosage compensation in gene circuits. *Science* **329**, 1656–1660 (2010).
56. J. Hose *et al.*, Dosage compensation can buffer copy-number variation in wild yeast. *eLife* **4**, e05462 (2015).
57. T. H. Segall-Shapiro, E. D. Sontag, C. A. Voigt, Engineered promoters enable constant gene expression at any copy number in bacteria. *Nat. Biotechnol.* **36**, 352–358 (2018).
58. Y. Voicheck, R. Bar-Ziv, N. Barkai, Expression homeostasis during DNA replication. *Science* **351**, 1087–1090 (2016).
59. J. Desponds, M. Vergassola, A. M. Walczak, A mechanism for *hunchback* promoters to readout morphogenetic positional information in less than a minute. *eLife* **9**, e49758 (2020).
60. Y. Hwang *et al.*, Global increase in replication fork speed during a p57<sup>KIP2</sup>-regulated erythroid cell fate switch. *Sci. Adv.* **3**, e1700298 (2017).
61. L. S. Weinberger, A minimal fate-selection switch. *Curr. Opin. Cell Biol.* **37**, 111–118 (2015).